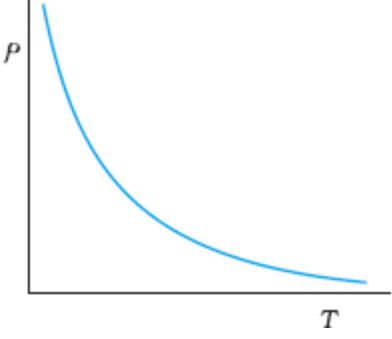
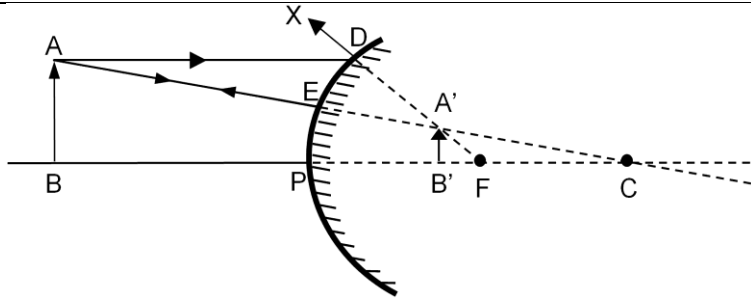


Marking Scheme

55/3/2

Q.No	Value Points/ Expected answers	Marks	Total Marks
1.		1	1
2.	The loss of the strength of the signal while propagating through a medium is called attenuation	1	1
3	Sphere A will be negatively charged Sphere B will be positively charged Alternatively- B will be similarly charged to the rod and A will be oppositely charged. <b style="text-align: center;">OR Sphere will be positively charged. Reason - Electrostatic Induction	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	1
4	No, K_{\max} becomes more than twice its initial value as $E_k = hv - \phi_0$	$\frac{1}{2} + \frac{1}{2}$	1
5.	$f_o \gg f_e$ Focal length of objective must be much greater than focal length of eyepiece OR Angle of minimum deviation decreases.	1 1	1
6	SECTION B <div style="border: 1px solid black; padding: 10px; width: fit-content; margin: auto;"> Showing by diagram 2 Alternatively Proof with mirror equation </div>		



Since rays diverge it is a virtual image

Alternatively

$$\frac{1}{f} + \frac{1}{v} = \frac{1}{u}$$

$$\frac{v}{f} = 1 + \frac{v}{u}$$

$$m = \frac{-v}{u} = 1 - \frac{v}{u} \text{ since } v < f \text{ always } m \text{ is positive and less than } 1$$

So, the image is always virtual

1 ½

½

1

1

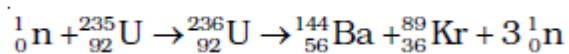
2

7.

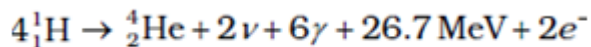
(i) Distinguishing property	1
(ii) Example for each	½ + ½

Nuclear Fission	Nuclear fusion
A heavy nucleus splits into two or more lighter nuclei with the release of energy	Two light nuclei combine to form a heavy nucleus with release of energy.

Example for Nuclear fusion



Example for Nuclear fission



1

½+½

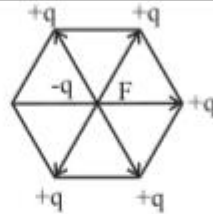
2

<p>8.</p>	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px;">(i)Formula</td> <td style="text-align: right; padding: 5px;">½</td> </tr> <tr> <td style="padding: 5px;">(ii)Ratio of wavelength emitted</td> <td style="text-align: right; padding: 5px;">1½</td> </tr> </table> $\frac{1}{\lambda} = R \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$ $\frac{1}{\lambda_1} = R \left[\frac{1}{2^2} - \frac{1}{3^2} \right] \dots\dots\dots (i)$ $\frac{1}{\lambda_2} = R \left[\frac{1}{1^2} - \frac{1}{2^2} \right] \dots\dots\dots (ii)$ $\frac{(2)}{(1)} = \frac{\lambda_1}{\lambda_2} = \frac{27}{5}$ <p>Alternatively - If electrons jump from second excited state to first excited state and second excited to ground state respectively</p> $\frac{1}{\lambda} = R \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$ $\frac{1}{\lambda_1} = R \left[\frac{1}{2^2} - \frac{1}{3^2} \right]$ $\frac{1}{\lambda_2} = R \left[\frac{1}{1^2} - \frac{1}{3^2} \right]$ $\frac{\lambda_1}{\lambda_2} = \frac{32}{5}$	(i)Formula	½	(ii)Ratio of wavelength emitted	1½	<p>½</p> <p>½</p> <p>½</p> <p>½</p> <p>½</p> <p>½</p> <p>½</p> <p>½</p>	<p>2</p> <p>2</p>
(i)Formula	½						
(ii)Ratio of wavelength emitted	1½						

9.

- i) Diagram(or statement) for justification
 ii) Net force (expression)

1
 1



Alternatively

The forces due to the charges placed diagonally opposite at the vertices of hexagon, on the charge $-q$ cancel in pairs. Hence net force is due to one charge only.

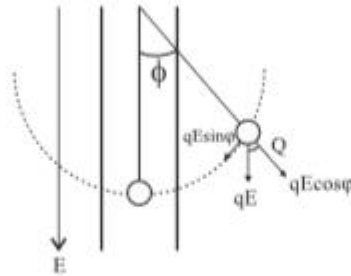
$$\text{Net Force } |\vec{F}| = \frac{1}{4\pi\epsilon_0} \frac{q^2}{r^2}$$

Ne

OR

- I) Diagram $\frac{1}{2}$
 ii) Derivation of period of oscillation $1\frac{1}{2}$

$1\frac{1}{2}$



Derivation

$$F_r = -qE \sin \phi \text{ (Restoring force)}$$

$$ma = -qE \sin \phi$$

when ϕ is small

$$ma = -qE \phi$$

$$m \frac{d^2x}{dt^2} = -qE \frac{x}{l}$$

$$\frac{d^2x}{dt^2} = -q \frac{E}{m} \frac{x}{l}$$

comparing with equation of linear SHM.

$$\frac{d^2x}{dt^2} = -\omega^2 x.$$

$$\omega = \sqrt{\frac{qE}{ml}}$$

2

1

1

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

2

$$T = \frac{2\pi}{\omega} = 2\pi\sqrt{\frac{ml}{qE}}$$

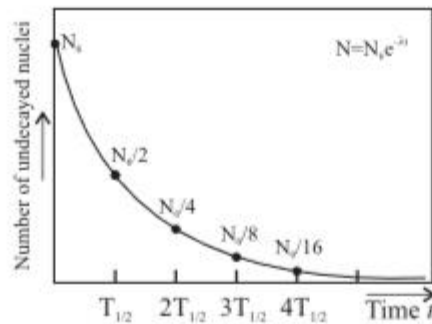
Alternatively - The student can use angular SHM expression also. Full marks to be awarded for correct answer even without intermediate steps..

½

10

i) Graph showing decay of radioactive nuclei	1
ii) Determination of half life and average life.	1

i)



- ii) From figure when $N = \frac{N_0}{2}$
 $t = T_{1/2}$ (half life)
 Average life $\tau = \frac{T_{1/2}}{0.693}$

1

2

½

½

11.

Formula	½
Calculation of Induced Voltage	1½

Induced voltage

$$\begin{aligned} |V| &= L \frac{dI}{dt} \\ \therefore |V| &= \mu_0 n^2 l a \frac{dI}{dt} \\ &= 4\pi \times 10^{-7} \times \left(\frac{10}{10^{-2}}\right)^2 \times 0.5 \times 1 \times 10^{-4} \times \frac{(2-1)}{0.1} \\ &= 6.28 \times 10^{-4} \text{V or } 0.628 \text{mV} \end{aligned}$$

OR

Calculation of (i) change of magnetic flux	1
(ii) induced emf	1

i) $\Delta\phi = \phi_2 - \phi_1 = 0 - NBA \cos\theta$
 $= 140 \times 0.09 \times 5 \times 10^{-4} \cos 0 = 63 \times 10^{-4} \text{Wb}$

½

½

½

½

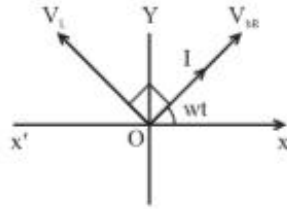
2

1

2

15

- | | |
|--|----|
| i) Explanation using phasor diagram | 1 |
| ii) Calculation of impedance | 1½ |
| iii) Calculation of potential difference | ½ |



- a) From phasor diagram it is clear that V_R is in phase with I and V_L is ahead of I in phase by $\pi/2$.

Hence V_L is ahead of V_R by $\pi/2$

- b) Let V be the effective potential difference across L-R circuit, therefore

$$V_{\text{rms}} = V = \sqrt{V_R^2 + V_L^2} = \sqrt{(160)^2 + (120)^2} = 200V$$

$$\therefore \text{Impedance of the circuit, } Z = \frac{V}{I} = \frac{200}{1} = 200\Omega$$

- c) For d.c. (constant voltage source) $V_L = 0$, therefore

$$\text{Potential difference in the circuit} = 200V$$

Alternatively, if the student takes it as a constant current source then the potential difference will be $= 160V = V_R$

OR

- | | |
|---|----|
| i) Naming the circuit element Y | ½ |
| ii) Calculation of r.m.s value of current | 1½ |
| iii) Effect of replacing a.c source by d.c source | 1 |

- a) Y is a capacitor.

- b) Phase angle, $\therefore \phi = \pi/4$, $\cos\phi = \frac{R}{Z}$

$$\Rightarrow Z = \frac{R}{\cos\phi} = \frac{R}{\cos(\pi/4)} = \frac{100}{1/\sqrt{2}} = 100\sqrt{2} = 141.4\Omega$$

$$I_{\text{r.m.s}} = \frac{V_{\text{r.m.s}}}{Z} = \frac{141V}{141.4\Omega} \cong 1A$$

- c) The current become zero.

1

½+½

½

½

½

½

½

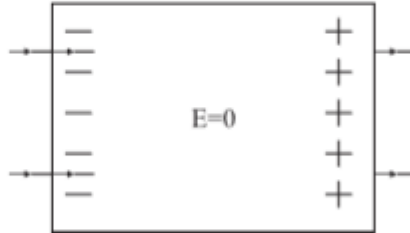
½

1

3

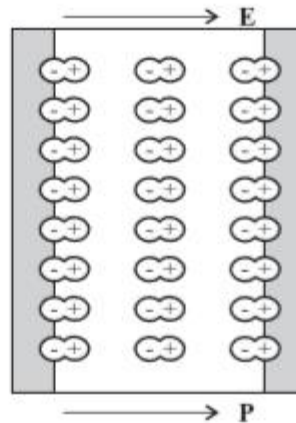
16

- | | |
|---|---|
| i) Explanation with diagram | 2 |
| ii) Definition of polarization and its expression for linear isotropic dielectric in terms of electric field. | 1 |



For conductor

Due to induction the free electrons collect on the left face of slab creating equal positive charge on the right face. Internal electric field is equal and opposite to external field; hence net electric field (inside the conductor) is zero.



For dielectric

Due to alignment of atomic dipoles (permanent or induced) along \vec{E} , the net electric field within the dielectric decreases.

- ii) The net dipole moment developed per unit volume in the presence of external electric field is called polarization vector \vec{P} .

Expression \therefore

$$\vec{P} = \chi_e \vec{E}$$

1/2

1/2

1/2

1/2

1/2

1/2

3

17

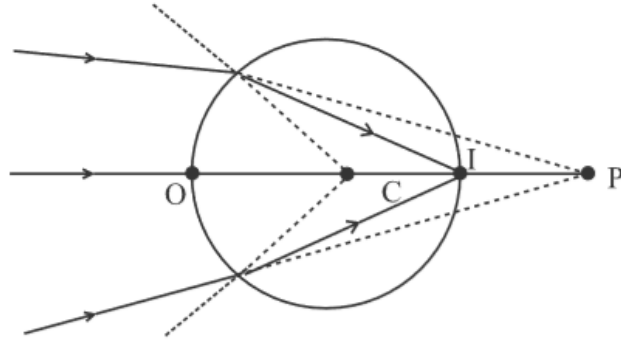
i) Calculation of new image position	2
ii) Ray diagram	1

a) $u = 20\text{cm}$, $n_2 = 1.5$, $n_1 = 1$, $R = 5\text{cm}$

Using $\frac{n_2}{v} - \frac{n_1}{u} = \frac{n_2 - n_1}{R}$

$$\frac{1.5}{v} - \frac{1}{20} = \frac{1.5 - 1}{5}$$

$$v = 10\text{ cm}$$



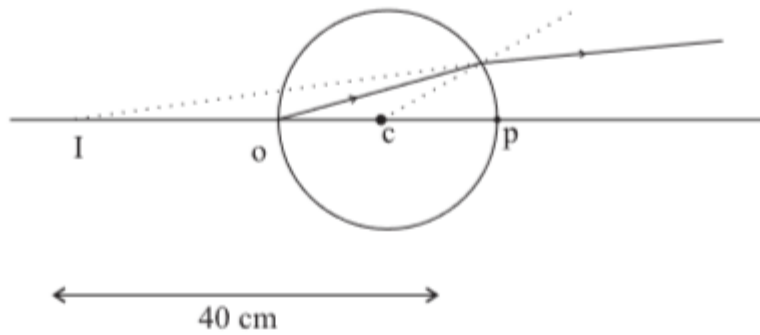
OR

Formula - 1
substitution and calculation - 1
Ray diagram - 1

$$\frac{n_1}{-u} + \frac{n_2}{v} = \frac{n_2 - n_1}{R}$$

$$\frac{1.5}{20} + \frac{1}{v} = \frac{1 - 1.5}{-10}$$

$$v = -40\text{cm}$$



½

1

½

1

1

½

½

1

3

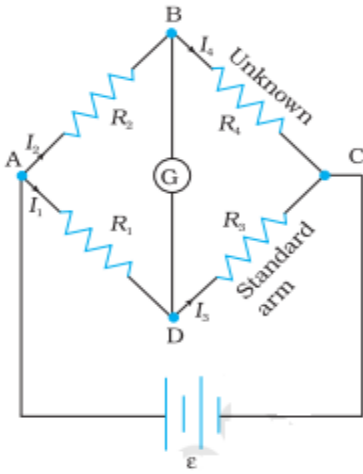
18

Obtaining balancing condition of wheatstone bridge

2 ½

One practical application

½



½

Applying kirchoff's loop rule to ADDB and CBDC

$$-I_1 R_1 + 0 + I_2 R_2 = 0$$

$$I_2 R_4 + 0 - I_3 R_3 = 0$$

$$\text{Since, } I_g = 0, I_3 = I_1, I_4 = I_2$$

$$\frac{I_1}{I_2} = \frac{R_4}{R_3} \quad \text{and} \quad \frac{I_1}{I_2} = \frac{R_2}{R_1}$$

$$\therefore \frac{R_4}{R_3} = \frac{R_2}{R_1} \quad (\text{Balance Condition})$$

½

½

½

½

A practical device using the principle of wheatstone bridge is meter bridge.

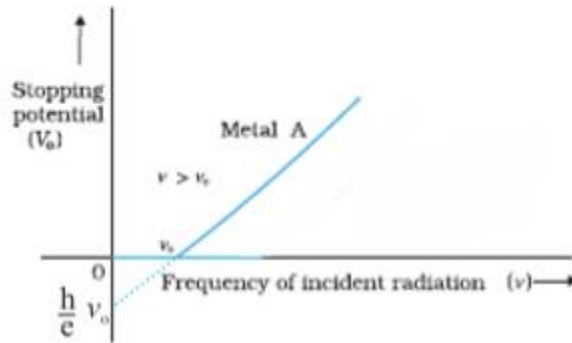
½

3

19.

- a) Graph showing variation of stopping potential with frequency - 1
 b) Showing the determination of
 (i) Threshold frequency - 1
 (ii) Planck's constant (from the graph) - 1

a.



b. From Einstein's Equation

$$eV_0 = h\nu - h\nu_0$$

$$V_0 = \frac{h}{e}\nu - \frac{h}{e}\nu_0$$

comparing

$$y = mx + c$$

(i) Threshold frequency ν_0 is the intercept along ν axis.

(Alternatively, intercept on V_0 axis, $c = \frac{h}{e}\nu_0$
 $\nu_0 = \frac{ec}{h}$)

(ii) Planck's constant $h = e \times \text{slope}$

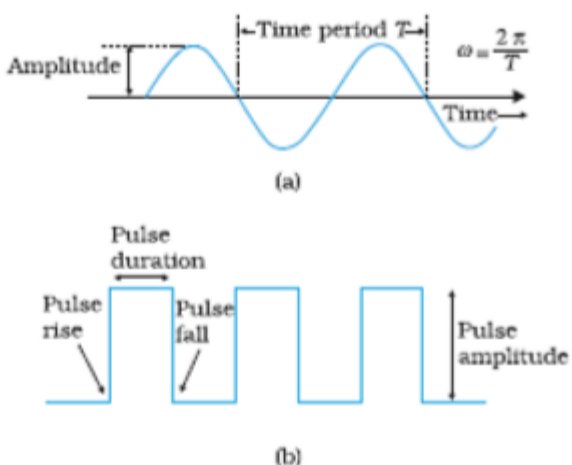
1

3

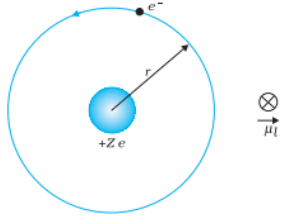
 $\frac{1}{2}$ $\frac{1}{2}$

1

	<p style="text-align: center;">OR</p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p>a. Explanation of emission of electron from a photosensitive surface - 1 b. Explanation and justification - 1 c. Finding the maximum KE - 1</p> </div> <p>a. When a photon of the energy $h\nu$ is absorbed by an electron in the photosensitive material, a part of the energy absorbed is used up in liberating it from the surface (the work function). The remaining energy appears as KE of the photoelectron.</p> <p>Alternatively: $K_{\max} = h\nu - \phi_0$</p> <p>if $h\nu \geq \phi_0$, k_{\max} is positive and electron is emitted</p> <p>b. Emission of electron will not take place. Energy $h\nu$, of a single photon, is less than the work function ϕ_0.</p> <p>(Alternatively - $k_{\max} = h\nu - \phi_0$ $h\nu < \phi_0$ so k_{\max} is negative; Hence no emission will take place.)</p> <p>c. $V_0 = 1.5 \text{ V}$ $k_{\max} = eV_0 = 1.6 \times 10^{-19} \times 1.5 = 2.4 \times 10^{-19} \text{ J}$</p> <p>[If a student just writes, $k_{\max} = 1.5 \text{ eV}$ award $\frac{1}{2}$ mark]</p>	<p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">1</p>	3
20.	<div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p>a. Meaning of bandwidth and importance - 1 b. Differentiation between analog & Digital signal - 1 c. Functions of transducers and repeaters - 1</p> </div> <p>a. Bandwidth of a signal is the range over which the frequencies in that signal vary.</p> <p>(Also accept bandwidth is the frequency range over which an equipment/device operates)</p>	$\frac{1}{2}$	

	<p>The knowledge of bandwidth helps in designing equipment used in communication/essential for communication.</p> <p>b. In digital communication, digital signals are used which have two discrete current or voltage values in a signal. Analog signals are used which have continuous current or voltage values in a signal.</p> <p>Alternatively, if a student draws the diagram of the digital signals and analog signals give these ($\frac{1}{2} + \frac{1}{2}$) mark.</p> <div style="text-align: center;">  <p>(a)</p> <p>(b)</p> </div> <p>c. A transducer converts one form of energy into another. A repeater enhances the range of a communication system.</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2} + \frac{1}{2}$</p>	<p>3</p>						
<p>21.</p>	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px;">a) Explanation of magnetic field lines being confined</td> <td style="text-align: right; padding: 5px;">$\frac{1}{2}$</td> </tr> <tr> <td style="padding: 5px;">b) Explanation of torque on a magnet due to itself</td> <td style="text-align: right; padding: 5px;">$\frac{1}{2} + \frac{1}{2}$</td> </tr> <tr> <td style="padding: 5px;">c) Obtaining expression</td> <td style="text-align: right; padding: 5px;">$1 \frac{1}{2}$</td> </tr> </table> <p>a) If field lines were extremely confined between two ends of a straight solenoid, the flux through the cross section at each end would be non zero. But the flux of field B through any closed surface must always be zero, For a toroid this difficulty is absent.</p> <p>b) No, There is no force on torque on an element due to the field produced by that element itself.</p>	a) Explanation of magnetic field lines being confined		$\frac{1}{2}$	b) Explanation of torque on a magnet due to itself	$\frac{1}{2} + \frac{1}{2}$	c) Obtaining expression	$1 \frac{1}{2}$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
a) Explanation of magnetic field lines being confined	$\frac{1}{2}$								
b) Explanation of torque on a magnet due to itself	$\frac{1}{2} + \frac{1}{2}$								
c) Obtaining expression	$1 \frac{1}{2}$								

c)



$$I = \frac{e}{T}, T = \frac{2\pi r}{v}$$

$$I = \frac{ev}{2\pi r}, \mu = I \pi r^2 = \frac{evr}{2}$$

½
½

3

22.

a. (i) Truth tables for P and Q - ½ + ½
 (ii) Truth tables for circuit - 1
 b. Explanation for why NOR gates are considered as universal gates - 1

a.

P

Q

(I)

A	Y
0	1
1	0

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

½ + ½

(ii)

A	B	Y
0	0	0
0	1	0
1	0	1
1	1	0

1

b. All basic logic gates can be realized by using NOR gates

(Also accept if the student draws the diagrams for getting OR & AND gates using NOR gates.)

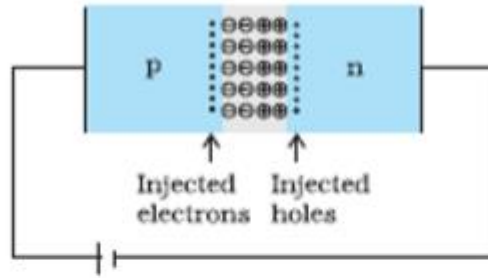
1

OR

a. Formation of potential barrier (with diagram) - 1½
 b. Circuit diagram and plotting graph - 1½

3

a.

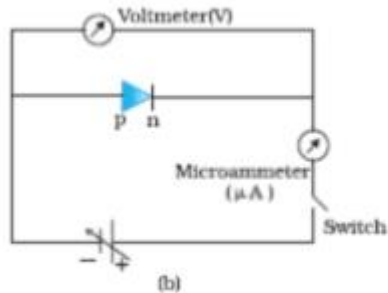
 $\frac{1}{2}$

During the formation of p - n junction diode; due to the concentration gradient across p and n sides of a diode, holes diffuse from p side to n side and electrons diffuse from n side to p side giving rise to development of immobile positive charges on the n side and the negative charges on the p side across the junction. Thus a potential barrier is formed at the junction.

1

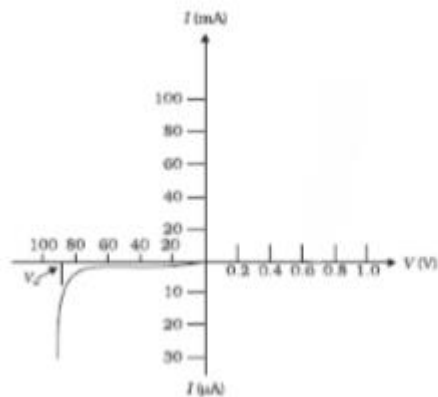
Alternatively: if a student explains with depletion region, award this 1 mark.

b.

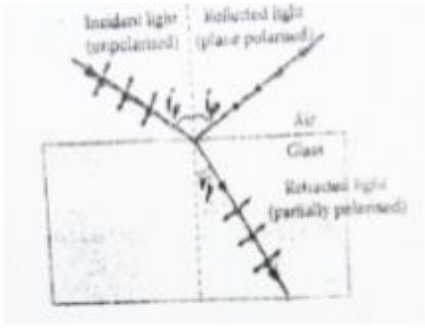


1

c.

 $\frac{1}{2}$

23.	<table border="1" data-bbox="250 237 1203 415"> <tr> <td data-bbox="274 258 1084 296">i) Generation of Eddy Current</td> <td data-bbox="1101 258 1117 296">1</td> </tr> <tr> <td data-bbox="274 310 1084 348">ii) Two examples of application</td> <td data-bbox="1101 310 1170 348">$\frac{1}{2} + \frac{1}{2}$</td> </tr> <tr> <td data-bbox="274 363 1084 401">iii) Method of minimizing</td> <td data-bbox="1101 363 1117 401">1</td> </tr> </table> <p data-bbox="215 436 1360 506">a) When the magnetic flux linked with a conductor changes with time, induced currents are set up inside the conductor.</p> <p data-bbox="215 527 1260 596">b) Induction furnace / Induction stove/Induction breaks/dead beat galvanometer (any two)</p> <p data-bbox="215 617 1167 646">c) By lamination/cutting shots (any one) eddy current can be minimized.</p>	i) Generation of Eddy Current	1	ii) Two examples of application	$\frac{1}{2} + \frac{1}{2}$	iii) Method of minimizing	1	<p data-bbox="1386 447 1403 476">1</p> <p data-bbox="1386 520 1456 550">$\frac{1}{2} + \frac{1}{2}$</p> <p data-bbox="1386 632 1403 661">1</p>	3
i) Generation of Eddy Current	1								
ii) Two examples of application	$\frac{1}{2} + \frac{1}{2}$								
iii) Method of minimizing	1								

<p>24</p>	<p>a. Diagram - ½ Explanation - 1 b. Calculation of (i) Polarizing angle - ½ (ii) Refractive index - 1</p>  <p>When unpolarized light propagates from a rarer into a denser medium, it gets partly reflected and partly refracted. If the reflected and refracted lights are perpendicular to each other, the reflected light gets polarized. (Alternatively if the student explains using Brewster's law award full marks.) (i) $i_p = 90 - r_p$ $i_p = 90 - 30 = 60^\circ$ (ii) $\mu = \tan i_p = \tan 60^\circ = \sqrt{3}$</p>	<p>½ 1 ½ 1</p>	
-----------	---	--	--

Section D

<p>25.</p>	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px;">i) Production of Interference pattern and explanation.</td> <td style="text-align: right; padding: 5px;">1+1</td> </tr> <tr> <td style="padding: 5px;">ii) Obtaining expression for intensity at the point P</td> <td style="text-align: right; padding: 5px;">1½</td> </tr> <tr> <td style="padding: 5px;">iii) Calculating wavelength of light</td> <td style="text-align: right; padding: 5px;">1½</td> </tr> </table> <p>a) No. Sustained interference pattern cannot be obtained Light waves emitted from a source undergoes abrupt phase changes in times of the order of 10^{-10} s. So light from two independent sources will not have fixed phase relationship and will be incoherent.</p>	i) Production of Interference pattern and explanation.	1+1	ii) Obtaining expression for intensity at the point P	1½	iii) Calculating wavelength of light	1½	<p>1 ½+½</p>	
i) Production of Interference pattern and explanation.	1+1								
ii) Obtaining expression for intensity at the point P	1½								
iii) Calculating wavelength of light	1½								

b) $x = \frac{\beta}{3}$, path difference = $\frac{\lambda}{3}$

$$\text{phase diff} = \frac{2\pi}{3}$$

$$I = I_0 \cos^2 \frac{\phi}{2}$$

$$I = I_0 \cos^2 \left(\frac{2\pi}{3 \times 2} \right) = I_0 \cos^2 \left(\frac{\pi}{3} \right)$$

$$I = I_0 \left(\frac{1}{4} \right) = \frac{I_0}{4}$$

½

½

½

c) Distance of 5th bright fringe from 2nd dark fringe

$$x = \frac{5 \lambda D}{d} - \frac{3 \lambda D}{2 d} = \frac{7 \lambda D}{2 d}$$

$$\lambda = \frac{2xd}{7D} = \frac{2 \times 4.13 \times 10^{-3} \times 0.5 \times 10^{-3}}{7 \times 1}$$

$$\lambda = 0.59 \times 10^{-6} \text{m} = 5900 \text{ \AA}$$

½

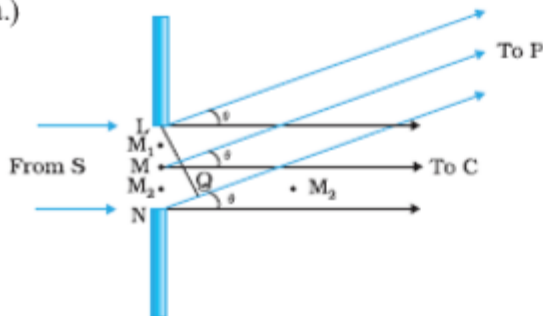
½

½

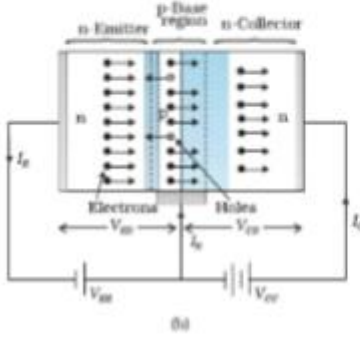
OR

i) Derivation of relation	2
ii) Effect on linear width of central maximum	½+½
iii) Determination of slit width	2

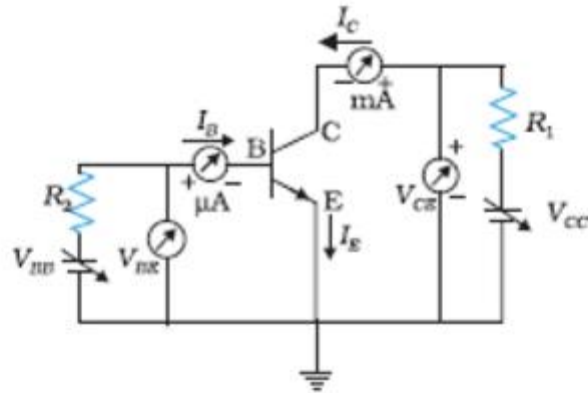
a.)



½

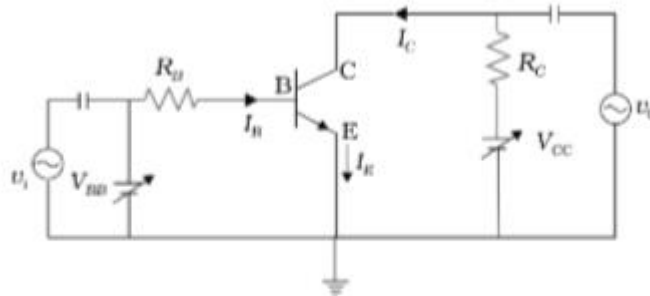
	<p>From diagram path difference between the waves from L and N $= a \sin\theta$</p> <p>When first minimum is obtained at P then path difference $= \lambda$</p> <p>[imagine the slit be divided into two halves, for each wavelets from first half of the slit has a corresponding wavelet from second half of the slit differing by a path of $\frac{\lambda}{2}$ and cancel each other]</p> <p>Condition for first minimum</p> <p>$\therefore \lambda = a \sin\theta$</p> <p>b.) $\beta_{cm} = \frac{2 \lambda D}{d}$</p> <p>(i) increases (ii) increases</p> <p>c.) $10 \frac{\lambda_c}{d} = 2 \frac{\lambda}{a}$</p> <p>$a = \frac{d}{5} = 0.2\text{mm}$</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p>	<p>5</p>
<p>26.</p>	<div style="border: 1px solid black; padding: 10px;"> <p>a. Circuit diagram and its working - 2 Explanation of low and high resistance at input and output respectively - 1</p> <p>b. Derivation of voltage gain - $1\frac{1}{2}$ Input and output phase relation. - $\frac{1}{2}$</p> </div> <p>a.</p> 	<p>1</p>	

(Also accept the following circuit diagram.



When Emitter Base junction is forward biased, electron from emitter enter the base where a few free charge carriers combine with the holes present in the base. As base is thin, most of the electron go into the collector, since collector junction is reverse biased, it gives rise to a collector current. Since Emitter-Base junction is forward biased, input resistance is low and base-collector is reversed biased, so output resistance is high.

b.



Applying Kirchoff's loop rule to input loop and taking variation

$$\Delta V_{BE} = \Delta I_B (R_B + r_i) \dots\dots\dots(1)$$

Output loop and taking variations

$$\Delta V_{CE} = - R_L \Delta I_C \dots\dots\dots(2)$$

$$\text{Voltage gain, } A_v = \frac{v_o}{v_i} = \frac{\Delta V_{CE}}{\Delta V_{BE}} = - \frac{R_L \Delta I_C}{\Delta I_B (R_B + r_i)} = - \beta_{ac} \frac{R_L}{r}$$

$$\text{Where, } R_B + r_i = r \dots\dots\dots(3)$$

$$\text{and } \beta_{ac} = \text{Current gain in C.E.} = \frac{\Delta I_C}{\Delta I_B}$$

The negative sign in equation (3) indicates that the input and output voltages are in opposite phase.

1

½ + ½

5

1

½

½

OR

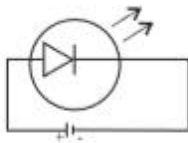
a) Two considerations for fabricating p-n junction diode used as LED	1
Order of band gap	1
Circuit diagram and action	1
b) V-I characteristics of LED	1
Two advantages of LED lamps over conventional lamps	½+½

- a) Important fabricating consideration
- i) Heavily doped
 - ii) Encapsulated with transparent cover.

½+½

For visible light:
order of band gap for LED = 1.8 eV to 3eV

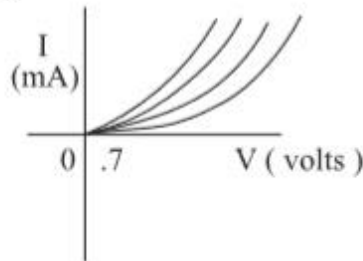
1



½

When the diode is forward biased, electron are sent from n side to p side and holes are sent from p side to n side and at the junction boundary, the excess minority carrier recombines with the majority carriers releasing energy in the form of photons.

½



1

Two advantage of LED over ordinary Lamps
Low operational voltage/Less power consumption / fast action / No warm up time required / Nearly monochromatic / Long life / ruggedness / fast switching capacity (Any two)

½ + ½

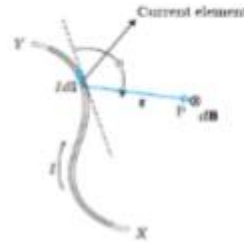
5

27.

- a. Statement of the law and expression for the magnetic field - 1+2
 b. Finding the magnitude and direction of magnetic field - 1½ +½

- a. According to Biot Savart law, the magnetic field due to a current element is given by

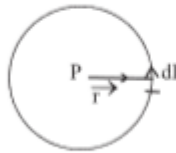
$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{l} \times \vec{r}}{r^3}$$



1

Alternatively award this 1 mark if a student makes statement of Biot Savart law.

Derivation of magnetic field



½

Magnetic field due to current element dl

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{l} \times \hat{r}}{r^2} \quad \text{where } \hat{r} \text{ is a unit vector along } \vec{r}$$

$$\vec{r} \perp d\vec{l}$$

Direction of $d\vec{B}$ is perpendicular, pointing outward.

½

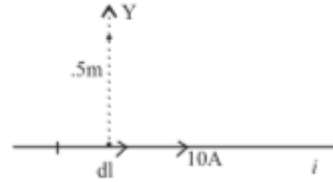
∴ Field due to the whole loop

$$\left| \vec{B} \right| = \int dB = \frac{\mu_0 I}{4\pi r^2} \int dl = \frac{\mu_0 I}{4\pi r^2} \times 2\pi r$$

$$\left| \vec{B} \right| = \frac{\mu_0 I}{2r}$$

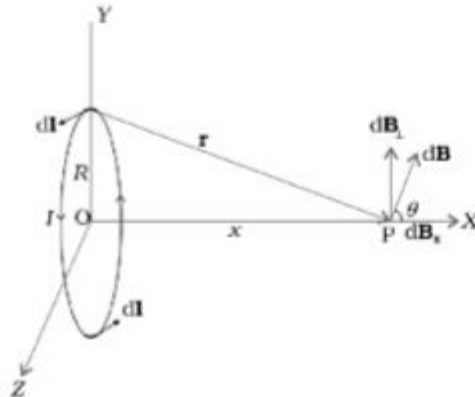
b.

$$\begin{aligned} \left| \vec{dB} \right| &= \frac{\mu_0 I}{4\pi} \frac{dl \sin\theta}{r^2} \\ &= \frac{4\pi \times 10^{-7}}{4\pi} \times \frac{10 \times (1 \times 10^{-2}) \times \sin 90^\circ}{(0.5)^2} \\ &= 4 \times 10^{-8} T \end{aligned}$$



OR

a) Derivation of expression with diagram	3
b) Calculation of magnitude of magnetic field at the center of the arc. Direction of field	1½ ½



According to Biot Savart law

½

½

½

1

½

5

1

$$|\vec{dB}| = \frac{\mu_0}{4\pi} \frac{I dl \sin 90^\circ}{|\vec{r}_1|^2}$$

Where $r_1 = \sqrt{x^2 + r^2}$

$$|\vec{dB}| = \frac{\mu_0}{4\pi} \frac{I dl}{(x^2 + r^2)^{3/2}}$$

Direction of \vec{dB} is perpendicular to $d\vec{l}$ and \vec{r}_1 .

It has components dB_x and dB_\perp . The components dB_\perp due to the whole coil cancel out in pairs.

Net field $B = \int dB_x = \int dB \cos\theta$

$$\vec{B} = \frac{\mu_0 I r^2}{2 (r^2 + x^2)^{3/2}} \hat{i}$$

b) $B = \frac{\mu_0 I}{4r}$

$$= \frac{4\pi \times 10^{-7} \times 5}{4 \times 2 \times 10^{-2}}$$

$$= 7.85 \times 10^{-5} \text{ T}$$

The field is directed inwards perpendicular to the plane of the page.

1/2

1/2

1

1/2

1/2

1/2

1/2