

QUESTION PAPER CODE 30/5/2
EXPECTED ANSWER/VALUE POINTS

SECTION – A

Question numbers 1 to 10 are multiple choice questions of 1 mark each.

You have to select the correct choice :

Q.No.

Marks

1. The value(s) of k for which the quadratic equation $2x^2 + kx + 2 = 0$ has equal roots, is

(a) 4 (b) ± 4 (c) -4 (d) 0

Ans: (b) ± 4

1

2. Which of the following is *not* an A.P.?

(a) $-1.2, 0.8, 2.8, \dots$ (b) $3, 3 + \sqrt{2}, 3 + 2\sqrt{2}, 3 + 3\sqrt{2}, \dots$

(c) $\frac{4}{3}, \frac{7}{3}, \frac{9}{3}, \frac{12}{3}, \dots$ (d) $\frac{-1}{5}, \frac{-2}{5}, \frac{-3}{5}, \dots$

Ans: (c) $\frac{4}{3}, \frac{7}{3}, \frac{9}{3}, \frac{12}{3}, \dots$

1

3. In Figure 1, from an external point P , two tangents PQ and PR are drawn to a circle of radius 4 cm with centre O . If $\angle QPR = 90^\circ$, then length of PQ is

(a) 3 cm
 (b) 4 cm
 (c) 2 cm
 (d) $2\sqrt{2}$ cm

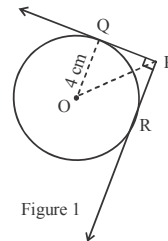


Figure 1

Ans: (b) 4 cm

1

4. The distance between the points $(m, -n)$ and $(-m, n)$ is

(a) $\sqrt{m^2 + n^2}$ (b) $m + n$
 (c) $2\sqrt{m^2 + n^2}$ (d) $\sqrt{2m^2 + 2n^2}$

Ans: (c) $2\sqrt{m^2 + n^2}$

1

5. The degree of the polynomial having zeroes -3 and 4 only is

(a) 2 (b) 1
 (c) More than 3 (d) 3

Ans: All the three options (a), (c) and (d) are acceptable

1 mark for any of the option (a), (c) or (d)

1

6. In Figure 2, ABC is an isosceles triangle, right-angled at C . Therefore

(a) $AB^2 = 2AC^2$
 (b) $BC^2 = 2AB^2$
 (c) $AC^2 = 2AB^2$
 (d) $AB^2 = 4AC^2$

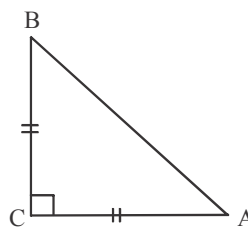


Figure 2

Ans: (a) $AB^2 = 2AC^2$

1

15. Simplest form of $(1 - \cos^2 A)(1 + \cot^2 A)$ is _____.

Ans: 1

1

Answer the following question numbers 16 to 20.

16. The LCM of two numbers is 182 and their HCF is 13. If one of the numbers is 26, find the other.

Ans: $\frac{182 \times 13}{26} = 91$

1/2+1/2

17. Form a quadratic polynomial, the sum and product of whose zeros are (-3) and 2 respectively.

Ans: $x^2 + 3x + 2$

1

OR

Can $(x^2 - 1)$ be a remainder while dividing $x^4 - 3x^2 + 5x - 9$ by $(x^2 + 3)$? Justify your answer with reasons.

Ans: No, degree of remainder $<$ degree of divisor

1

18. Find the sum of the first 100 natural numbers.

Ans: $\frac{100}{2}[2 + 99] = 5050$

1/2+1/2

19. Evaluate:

$2 \sec 30^\circ \times \tan 60^\circ$

Ans: $2 \times \frac{2}{\sqrt{3}} \times \sqrt{3}$
 $= 4$

1/2

1/2

20. In Figure 4, the angle of elevation of the top of a tower from a point C on the ground, which is 30 m away from the foot of the tower, is 30° . Find the height of the tower.

Ans: $\frac{AB}{30} = \frac{1}{\sqrt{3}} \Rightarrow AB = \frac{30}{\sqrt{3}}$ m or $10\sqrt{3}$ m

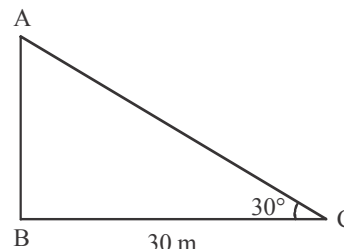


Figure 4

1/2+1/2

SECTION – B

Question numbers 21 to 26 carry 2 marks each.

21. Find the mode of the following distribution:

Marks:	0-10	10-20	20-30	30-40	40-50	50-60
Number of Students:	4	6	7	12	5	6

Ans: Modal class : 30 – 40

1/2

Mode = $L + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h = 30 + \frac{5}{12} \times 10$
 $= 34.17$

1

1/2

22. In Figure 5, a quadrilateral ABCD is drawn to circumscribe a circle. Prove that $AB + CD = BC + AD$.

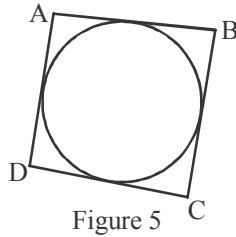


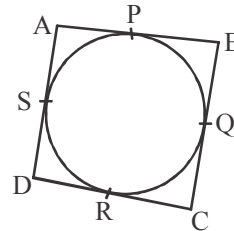
Figure 5

Ans: Let the circle touches the sides AB, BC, CD and AD at P, Q, R and S respectively.

$$\therefore \left. \begin{array}{l} AP = AS \\ BP = BQ \\ DR = DS \\ CR = CQ \end{array} \right\}$$

adding, we get $(AP + BP) + (DR + CR) = (AS + DS) + (BQ + CQ)$

$$\therefore AB + CD = BC + AD$$



OR

In Figure 6, find the perimeter of $\triangle ABC$, if $AP = 12$ cm.

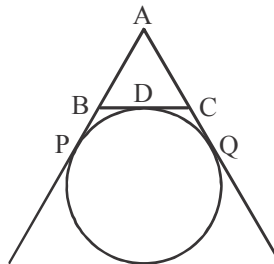


Figure 6

$$\text{Ans: } \left. \begin{array}{l} AP = AB + BP = AB + BD \\ AQ = AC + CQ = AC + CD \end{array} \right\}$$

$$\Rightarrow AP + AQ = AB + AC + (BD + CD) = AB + AC + BC$$

But $AP = AQ \therefore 2 AP = \text{Perimeter of } ABC$

$$\therefore \text{Perimeter} = 2(12) = 24 \text{ cm}$$

23. How many cubes of side 2 cm can be made from a solid cube of side 10 cm?

$$\begin{aligned} \text{Ans: No. of cubes} &= \frac{10 \times 10 \times 10}{2 \times 2 \times 2} \\ &= 125 \end{aligned}$$

1/2

1

1/2

1

1/2

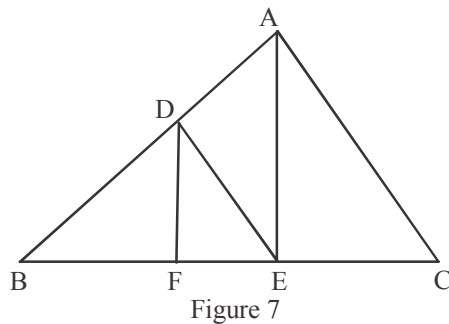
1/2

1

1

24. In the given Figure 7, $DE \parallel AC$ and $DF \parallel AE$.

Prove that $\frac{BF}{FE} = \frac{BE}{EC}$.



Ans: In $\triangle ABE$, $DF \parallel AE$, $\therefore \frac{BD}{AD} = \frac{BF}{EF}$... (i)

In $\triangle ABC$, $DE \parallel AC$, $\therefore \frac{BD}{AD} = \frac{BE}{EC}$... (ii)

From (i) and (ii) $\frac{BF}{FE} = \frac{BE}{EC}$ 1/2

25. Show that $5 + 2\sqrt{7}$ is an irrational number, where $\sqrt{7}$ is given to be an irrational number.

Ans: Let us assume that $5 + 2\sqrt{7}$ is not an irrational number.

$\therefore 5 + 2\sqrt{7}$ is a rational number p i.e. $5 + 2\sqrt{7} = p$ 1

$\Rightarrow \sqrt{7} = \frac{p-5}{2}$ 1/2

Which is a contradiction as RHS is a rational but LHS is irrational.

Hence $5 + 2\sqrt{7}$ can not be rational, so irrational. 1/2

OR

Check whether 12^n can end with the digit 0 for any natural number n.

Ans: Prime factors of 12 are $2 \times 2 \times 3$ 1

Since 5 is not a factor, so 12^n can not end with 0. 1

26. If A, B and C are interior angles of a $\triangle ABC$, then show that

$$\cot\left(\frac{B+C}{2}\right) = \tan\left(\frac{A}{2}\right).$$

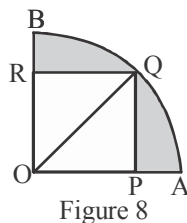
Ans: $A + B + C = 180^\circ$, $\therefore \frac{B+C}{2} = 90^\circ - \frac{A}{2}$ 1

$\therefore \cot\left(\frac{B+C}{2}\right) = \cot\left(90^\circ - \frac{A}{2}\right) = \tan\frac{A}{2}$ 1

SECTION – C

Question numbers 27 to 34 carry 3 marks each.

27. In Figure-8, a square OPQR is inscribed in a quadrant OAQB of a circle. If the radius of the circle is $6\sqrt{2}$ cm, find the area of shaded region.



Ans: Let side of square be 'a' cm $\therefore a^2 + a^2 = (6\sqrt{2})^2 \Rightarrow a = 6$ cm

$$\begin{aligned} \therefore \text{Area of shaded region} &= \pi r^2 \frac{90}{360} - a^2 = \frac{22}{7} \times (6\sqrt{2})^2 \cdot \frac{1}{4} - 36 \\ &= \frac{396 - 252}{7} = \frac{144}{7} \text{ cm}^2 \text{ or } 20.57 \text{ cm}^2 \end{aligned}$$

28. Construct a ΔABC with sides $BC = 6$ cm, $AB = 5$ cm and $\angle ABC = 60^\circ$.

Then construct a triangle whose sides are $\frac{3}{4}$ of the corresponding sides of ΔABC .

Ans: Constructing ΔABC with given dimensions
Constructing the similar triangle.

OR

Draw a circle of radius 3.5 cm. Take a point P outside the circle at a distance of 7 cm from the centre of the circle and construct a pair of tangents to the circle from that point.

Ans: Drawing a circle of radius 3.5 cm and centre O, and taking a point P such that $OP = 7$ cm
Constructing two tangents.

29. Prove that:

$$\frac{2 \cos^3 \theta - \cos \theta}{\sin \theta - 2 \sin^3 \theta} = \cot \theta$$

Ans: L.H.S. = $\frac{\cos \theta (2 \cos^2 \theta - 1)}{\sin \theta (1 - 2 \sin^2 \theta)}$

$$= \frac{\cos \theta [2(1 - \sin^2 \theta) - 1]}{\sin \theta (1 - 2 \sin^2 \theta)}$$

$$= \frac{\cos \theta (1 - 2 \sin^2 \theta)}{\sin \theta (1 - 2 \sin^2 \theta)}$$

$$= \cos \theta = \text{R.H.S.}$$

1

$1 + \frac{1}{2}$

$\frac{1}{2}$

1

2

1

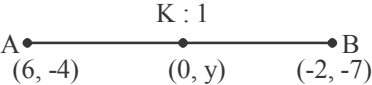
2

$\frac{1}{2}$

1

1

$\frac{1}{2}$

<p>30.</p>	<p>A fraction becomes $\frac{1}{3}$ when 1 is subtracted from the numerator and it becomes $\frac{1}{4}$ when 8 is added to its denominator. Find the fraction.</p> <p>Ans: Let the fraction be $\frac{x}{y}$</p> $\therefore \frac{x-1}{y} = \frac{1}{3}, \frac{x}{y+8} = \frac{1}{4}$ $\Rightarrow 3x - y = 3, 4x - y = 8$ <p>Solving to get $x = 5, y = 12 \therefore$ Fraction is $\frac{5}{12}$</p> <p style="text-align: center;">OR</p> <p>The present age of a father is three years more than three times the age of his son. Three years hence the father's age will be 10 years more than twice the age of the son. Determine their present ages.</p> <p>Ans: Let the present age of son be x years</p> <p>\therefore Father's present age = $(3x + 3)$ years.</p> <p>3 years hence, Son's age = $(x + 3)$ years and father's age = $(3x + 6)$ years</p> $\therefore 3x + 6 = 2(x + 3) + 10$ $\Rightarrow x = 10 \therefore \text{Son's age} = 10 \text{ years,}$ <p style="padding-left: 40px;">Father's age = 33 years</p>	<p>1/2</p> <p>1/2+1/2</p> <p>1/2</p> <p>1</p>
<p>31.</p>	<p>Using Euclid's Algorithm, find the largest number which divides 870 and 258 leaving remainder 3 in each case.</p> <p>Ans: HCF of $(870 - 3)$ and $(258 - 3)$</p> $= 867 \text{ and } 255$ $\left. \begin{aligned} 867 &= 255 \times 3 + 102 \\ 255 &= 102 \times 2 + 51 \\ 102 &= 51 \times 2 + 0 \end{aligned} \right\}$ <p>\therefore HCF = 51</p>	<p>1</p> <p>1/2</p> <p>1</p> <p>1/2</p>
<p>32.</p>	<p>Find the ratio in which the y-axis divides the line segment joining the points $(6, -4)$ and $(-2, -7)$. Also find the point of intersection.</p> <p>Ans: Let the point $P(0, y)$ on y-axis divides the line segment AB in $K : 1$</p>  $\therefore 0 = \frac{-2K + 6}{K + 1} \Rightarrow K = 3 \therefore \text{Ratio is } 3 : 1$ <p>Also, $y = \frac{3(-7) + 1(-4)}{3 + 1} = \frac{-25}{4} \therefore$ Point of intersection is $\left(0, \frac{-25}{4}\right)$</p>	<p>1</p> <p>1</p> <p>1</p>

OR

Show that the points A(7, 10), B(-2, 5) and C(3, -4) are vertices of an isosceles right triangle.

Ans: Let the points be A(7, 10), B(-2, 5) and C(3, -4)

$$AB = \sqrt{(-2-7)^2 + (5-10)^2} = \sqrt{106}$$

$$BC = \sqrt{(3+2)^2 + (-4-5)^2} = \sqrt{106}$$

$$AC = \sqrt{(3-7)^2 + (-4-10)^2} = \sqrt{212}$$

$$AB = BC \text{ and } AC^2 = AB^2 + BC^2$$

Hence ABC is isosceles right triangle.

33. In an A.P. given that the first term (a) = 54, the common difference (d) = -3, and the n^{th} term (a_n) = 0. Find n and sum of first n terms (S_n) of the A.P.

Ans: $a_n = 0$

$$54 + (n-1)(-3) = 0$$
$$n = 19$$

$$S_{19} = \frac{19}{2}(54+0)$$
$$= 19 \times 27 = 513$$

34. Read the following passage and answer the questions given at the end:

Diwali Fair

A game in a booth at Diwali fair involves using of spinner first. Then, if the spinner stops at an even number, the player is allowed to pick a marble from bag. The spinner and the marbles in the bag are represented in Figure-9

Prizes are given, when a black marble is picked. Shweta plays the game once.

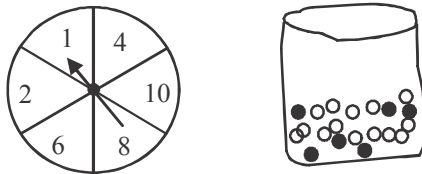


Figure 9

- (i) What is the probability that she will be allowed to pick a marble from the bag?
- (ii) Suppose she is allowed to pick a marble from the bag, what is the probability of getting a prize, when it is given that the bag contains 20 balls out of which 6 are black?

Ans: (i) $P(\text{she will be allowed to pick a marble}) = \frac{5}{6}$

(ii) $P(\text{getting a prize}) = \frac{6}{20}$ or $\frac{3}{10}$

Both answers $\frac{6}{20}$ or $\frac{0}{20}$ for part (ii) in Q34 are to be treated correct as the bag contains marbles only.

1

1/2

1/2

1

1/2

1

1

1/2

1 1/2

1 1/2

SECTION – D

Question numbers 35 to 40 carry 4 marks each.

- 35.** Sum of the areas of 2 squares is 544 m^2 . If the difference of their perimeter is 32 m, find the sides of two squares.

Ans: Let 'a' and 'b' be the sides of two squares, with $a > b$.

$$\text{then } a^2 + b^2 = 544 \text{ and } 4a - 4b = 32$$

$$\text{or } a - b = 8 \therefore a = b + 8$$

$$\therefore (b + 8)^2 + b^2 = 544 \Rightarrow 2b^2 + 16b - 480 = 0$$

$$\therefore b^2 + 8b - 240 = 0 \Rightarrow (b + 20)(b - 12) = 0 \Rightarrow b = 12$$

$$b = 12 \text{ m} \Rightarrow a = 12 + 8 = 20 \text{ m}$$

OR

A motorboat whose speed is 18 km/hr in still water takes 1 hour more to go 24 km upstream than to return downstream to the same spot. Find the speed of the stream.

Ans: Let speed of the stream be x km/h

$$\frac{24}{18 - x} - \frac{24}{18 + x} = 1$$

$$\Rightarrow 24(2x) = 324 - x^2 \text{ or } x^2 + 48x - 324 = 0$$

$$\Rightarrow (x + 54)(x - 6) = 0 \Rightarrow x = 6$$

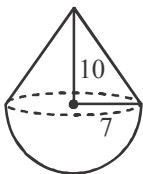
$$\therefore \text{Speed of the stream} = 6 \text{ km/h}$$

- 36.** A solid toy in the form of a hemisphere surmounted by a right circular cone of same radius. The height of the cone is 10 cm and the radius of its base is 7 cm. Determine the volume of the toy. Also find the area of the coloured sheet required to cover the toy.

(Use $\pi = \frac{22}{7}$ and $\sqrt{149} = 12.2$)

Ans: Volume of toy = $\frac{2}{3}\pi(7)^3 + \frac{1}{3}\pi(7)^2 \times 10 \text{ cm}^3$

$$= \frac{1}{3} \times \frac{22}{7} \times 49(14 + 10) = 1232 \text{ cm}^3$$



$$\begin{aligned} \text{Area of Sheet} &= \text{Surface area} = 2\pi(7)^2 + \pi(7)\sqrt{10^2 + 7^2} \\ &= 308 + 22 \times 12.2 = 576.4 \text{ cm}^2 \end{aligned}$$

- 37.** For the following data, draw a 'less than' ogive and hence find the median of the distribution.

Age							
(In years):	0-10	10-20	20-30	30-40	40-50	50-60	60-70
Number of persons:	5	15	20	25	15	11	9

$1 + \frac{1}{2}$

1

1

$1/2$

2

1

1

1

1

1

1

Ans: The points to be plotted for less than ogive are
 (10, 5), (20, 20), (30, 40), (40, 65), (50, 80), (60, 91), (70, 100)
 Drawing the ogive
 Getting median = 34 (approx)

OR

The distribution given below shows that the number of wickets taken by bowler in one-day cricket matches. Find the mean and the median of the number of wickets taken.

Number of wickets :	20-60	60-100	100-140	140-180	180-220	220-260
Number of bowlers :	7	5	16	12	2	3

Ans:

No. of wickets :	20-60	60-100	100-140	140-180	180-220	220-260	Sum
(f_i) No. of bowlers :	7	5	16	12	2	3	45
x_i	40	80	120	160	200	240	
u_i	-2	-1	0	1	2	3	
$f_i x_i$	-14	-5	0	12	4	9	6
cf	7	12	28	40	42	45	

$$\text{Mean} = a + \frac{\sum f_i u_i}{\sum f_i} \times h = 120 + \frac{6 \times 40}{45} = 125.33$$

$$\text{Median} = l + \frac{\frac{N}{2} - c}{f} \times h = 100 + \frac{22.5 - 12}{16} \times 40 = 126.25$$

38. From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top of a 20 m high building are 45° and 60° respectively. Find the height of the tower (Use $\sqrt{3} = 1.73$)

Ans: Let h be the height of the tower

In right $\triangle ABD$

$$\left. \begin{aligned} \frac{20}{x} &= \tan 45^\circ \\ x &= 20 \text{ m} \end{aligned} \right\}$$

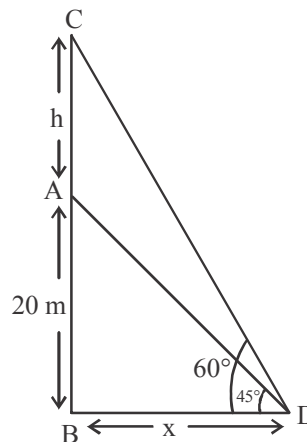
In right $\triangle CBD$

$$\frac{h+20}{20} = \tan 60^\circ$$

$$h+20 = 20\sqrt{3}$$

$$h = 20(\sqrt{3} - 1)$$

$$= 20 \times 0.73 = 14.60 \text{ m}$$



2
 $1 + \frac{1}{2}$
 $\frac{1}{2}$

$\frac{1}{2}$
 $\frac{1}{2}$
 $\frac{1}{2}$

$1 + \frac{1}{2}$

1

cor. fig. 1

1

1

$\frac{1}{2}$

$\frac{1}{2}$

<p>39.</p>	<p>Prove that in a right-angled triangle, the square of the hypotenuse is equal to the sum of the squares of the two sides.</p> <p>Ans: For correct Given, To Prove, Construction and figure</p> <p>For correct proof</p>	<p>$\frac{1}{2} \times 4 = 2$</p> <p>2</p>
<p>40.</p>	<p>Obtain other zeroes of the polynomial</p> $P(x) = 2x^4 - x^3 - 11x^2 + 5x + 5$ <p>If two of its zeroes are $\sqrt{5}$ and $-\sqrt{5}$.</p> <p>Ans: Since $\sqrt{5}$ and $-\sqrt{5}$ are zeroes of $p(x)$, so $(x - \sqrt{5})$ and $(x + \sqrt{5})$ are factors of $p(x)$. Thus $(x^2 - 5)$ is a factor of $p(x)$.</p> $(2x^4 - x^3 - 11x^2 + 5x + 5) \div (x^2 - 5) = 2x^2 - x - 1$ $2x^2 - x - 1 = (2x + 1)(x - 1)$ <p>\therefore Other zeroes of $p(x)$ are $1, -\frac{1}{2}$</p> <p style="text-align: center;">OR</p> <p>What minimum must be added to $2x^3 - 3x^2 + 6x + 7$ so that the resulting polynomial will be divisible by $x^2 - 4x + 8$?</p> <p>Ans:</p> $ \begin{array}{r} \overline{) 2x^3 - 3x^2 + 6x + 7} \\ \underline{2x^3 - 8x^2 + 16x} \\ 5x^2 - 10x + 7 \\ \underline{5x^2 - 20x + 40} \\ 10x - 33 \end{array} $ <p>\therefore We have to add $(33 - 10x)$</p>	<p>1</p> <p>$1\frac{1}{2}$</p> <p>1</p> <p>$1/2$</p> <p>3</p> <p>1</p>